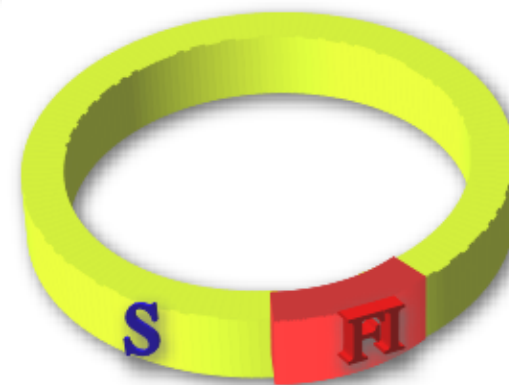
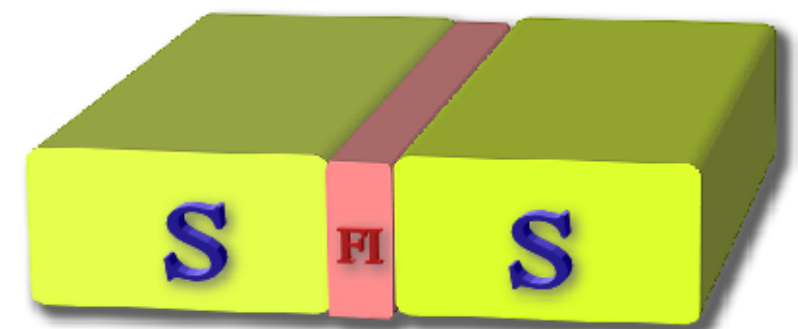
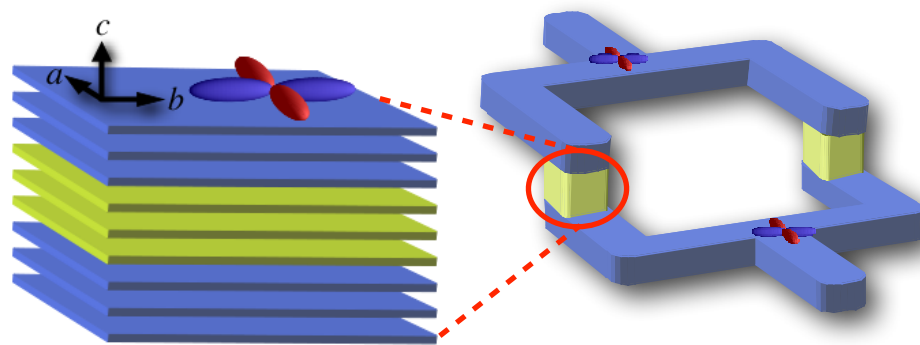


Physics of superconductor/ferromagnet junctions



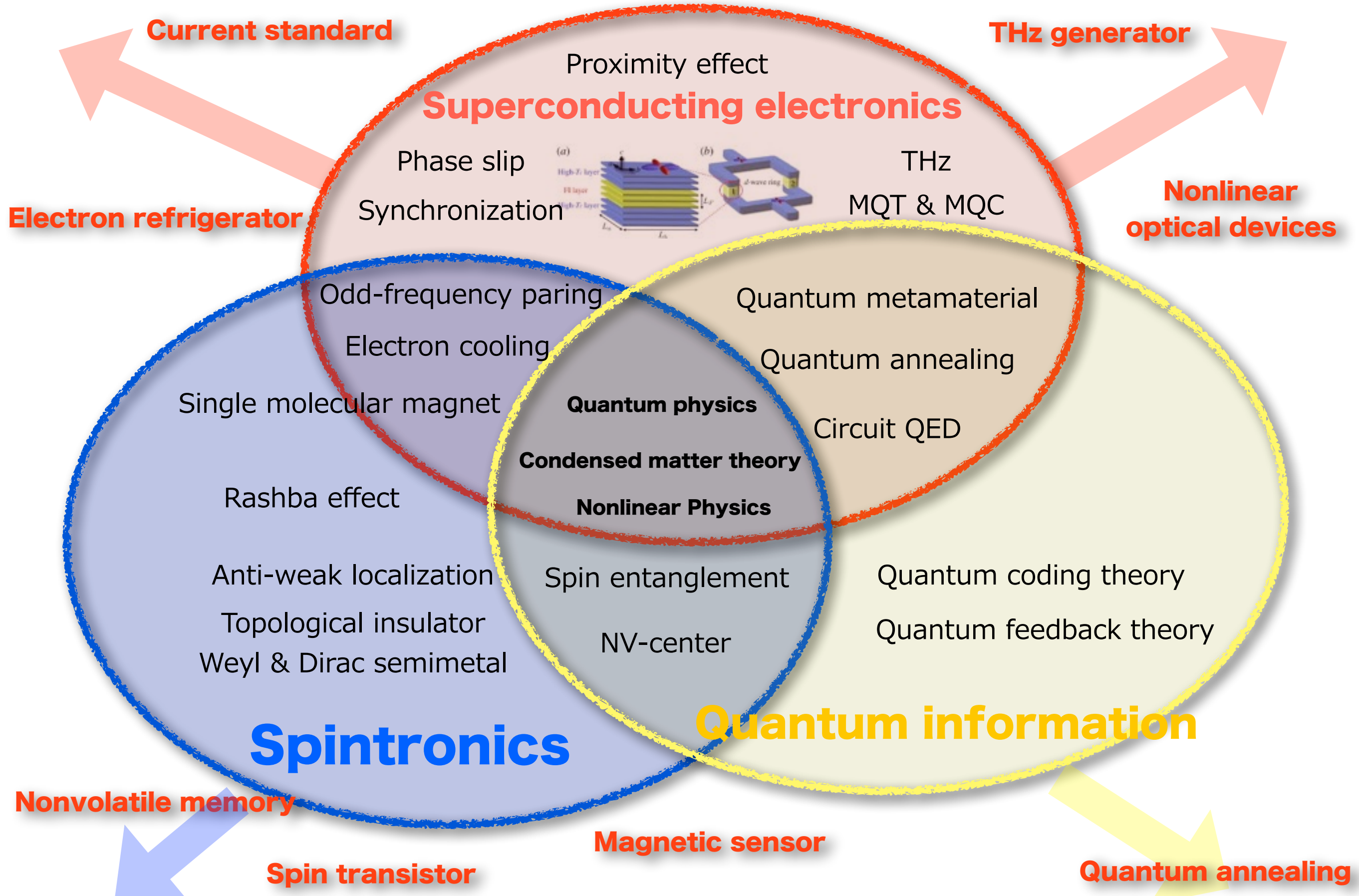
Shiro Kawabata

National Institute of Advanced Industrial Science & Technology (**AIST**), JAPAN



Research field: Overview

From basic to **application**



Collaboration with Dr. Vasenko (2010~)



[S. Kawabata](#), [A. S. Vasenko](#), A. Ozaeta, F. S. Bergeret & F. W. J. Hekking

"Heat transport and electron cooling in ballistic normal-metal/spin-filter/superconductor junctions"

Journal of Magnetism and Magnetic Materials 383 (2015) 157

[A. S. Vasenko](#), [S. Kawabata](#), A. Ozaeta, A. Golubov, F. S. Bergeret & F. W. J. Hekking

"Detection of small exchange fields in S/F structures"

Journal of Magnetism and Magnetic Materials 383 (2015) 175

[S. Kawabata](#), A. Ozaeta, [A. S. Vasenko](#), F. W. J. Hekking & F. S. Bergeret

"Efficient electron refrigeration using superconductor/spin-filter devices"

Appl. Phys. Lett. 103 (2013) 032602

[A. S. Vasenko](#), A. Ozaeta, [S. Kawabata](#), F. W. J. Hekking & F. S. Bergeret

"Andreev current and subgap conductance of spin-valve SFF structures"

J Supercond. Nov. Mag. 26 (2013) 1951

[S. Kawabata](#), Y. Tanaka, A. Golubov, [A. S. Vasenko](#) & Y. Asano

"Spectrum of Andreev bound states in Josephson junctions with a ferromagnetic insulator"

J Supercond. Nov. Mag. 324 (2012) 3467

[S. Kawabata](#), Y. Tanaka, A. A. Golubov, [A. S. Vasenko](#), S. Kashiwaya & Y. Asano

"Tunneling Hamiltonian description of the atomic-scale $0-\pi$ transition in superconductor/ferromagnetic-insulator junctions", Physica C 471 (2011) 1199

[A. S. Vasenko](#), [S. Kawabata](#), A. Golubov, M. Y. Kupriyanov, C. Lacroix, F. S. Bergeret & F. W. J. Hekking

"Current-voltage characteristics of tunnel Josephson junctions with a ferromagnetic interlayer"

Phys. Rev. B 84 (2011) 024524

A. [S. Vasenko](#), [S. Kawabata](#), A. Golubov & F. W. J. Hekking,

"Dissipative current in SIFS Josephson junctions"

Physica C 470 (2010) 863

Contents

1. Superconducting spintronics with **Ferromagnetic Metals**

- Josephson effect & Proximity effect
- **Josephson π junction**
- Applications
- Long range triplet Josephson effect

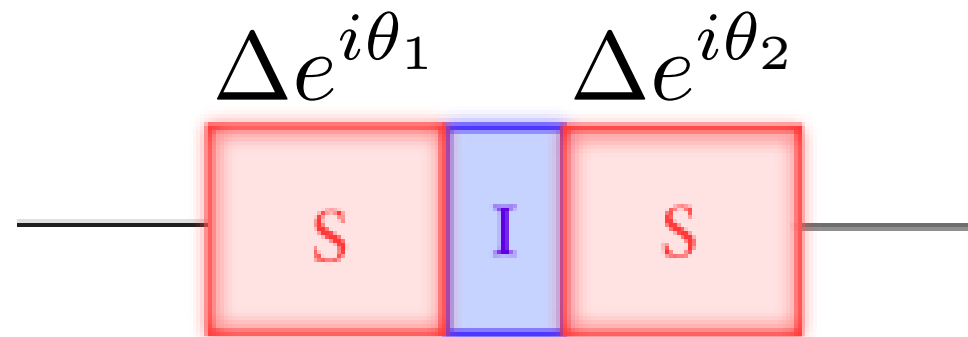
2. Superconducting spintronics with **Ferromagnetic Insulators**

- Ferromagnetic insulator & Spin-filtering effect
- **Atomic scale $0-\pi$ transition**
- Experiments
- Applications

3. Summary

Josephson junction

Weakly coupled two superconductors



DC current can flow without bias voltage

Josephson current (= tunneling of cooper pairs)

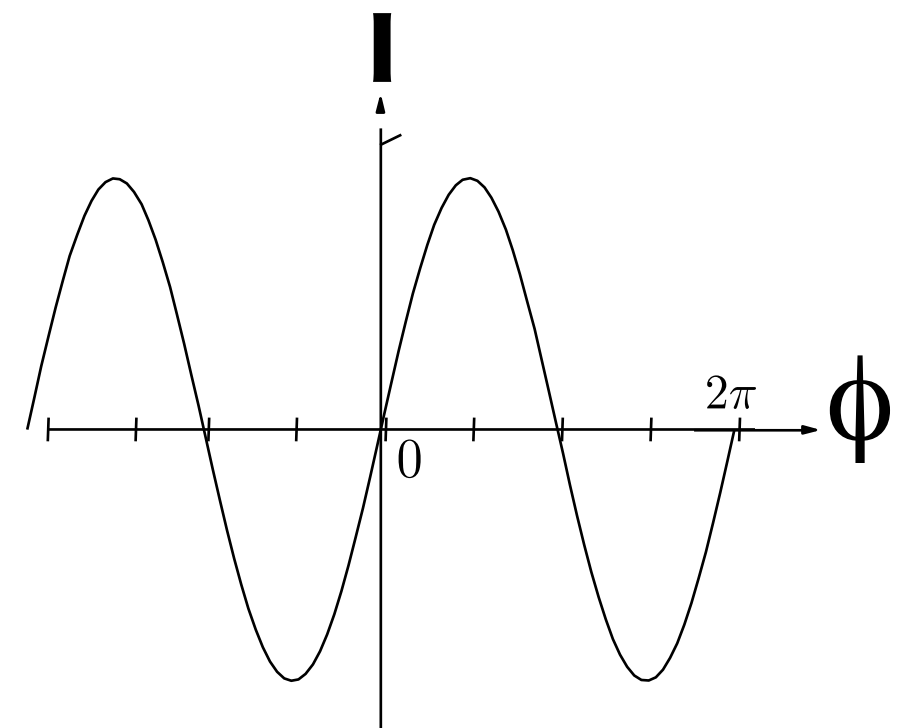
DC Josephson effect

$$I = I_C \sin \phi$$

I_c: Critical current

Driving force = phase difference in the macroscopic wave function

$$\phi = \theta_1 - \theta_2$$



π -junction in S/FM/S systems

Buzdin, Rev. Mod. Phys. 77 (05) 935

Eschrig, Phys. Today 64 (11) 43



FM : **F**erromagnetic **M**etal (Fe, Co, ...)

Exchange field



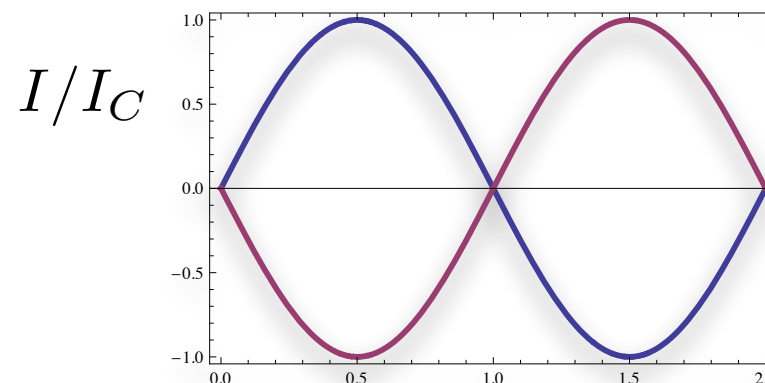
Non-zero momentum due to the spin exchange splitting in FMs



Pair-amplitude oscillation



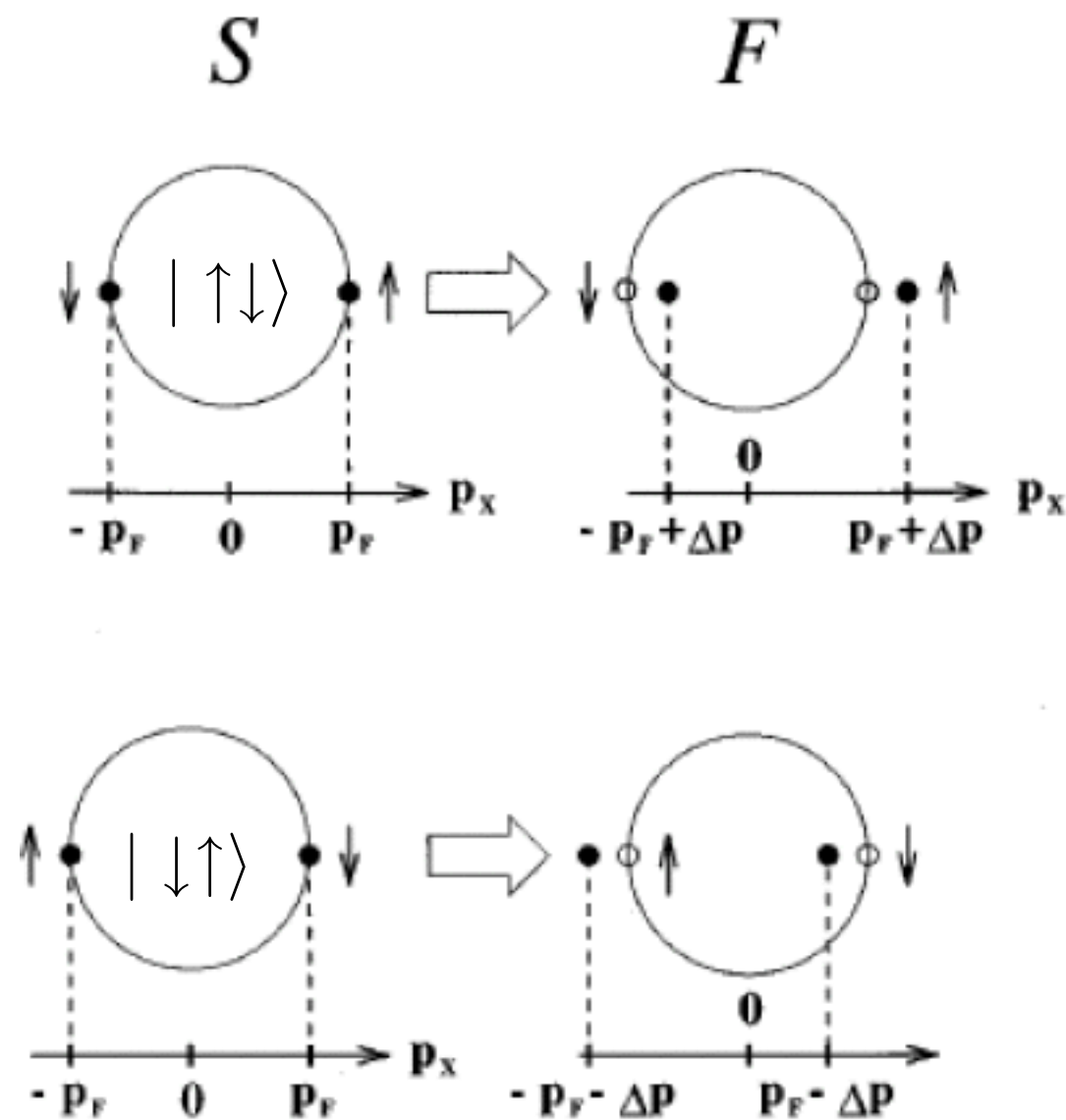
Josephson Current $I = -I_C \sin \phi = I_C \sin(\phi + \pi)$



π -junction $I = -I_C \sin \phi$
 ϕ
0-junction $I = +I_C \sin \phi$
Conventional

Cooper pair in S/FM hybrids

E. A. Demler et al., Phys. Rev. B, 55, 15174 (1997)



Cooper pair in S $|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle$

$$|\uparrow\downarrow\rangle \rightarrow e^{ix\Delta p} |\uparrow\downarrow\rangle$$

$$|\downarrow\uparrow\rangle \rightarrow e^{-ix\Delta p} |\downarrow\uparrow\rangle$$

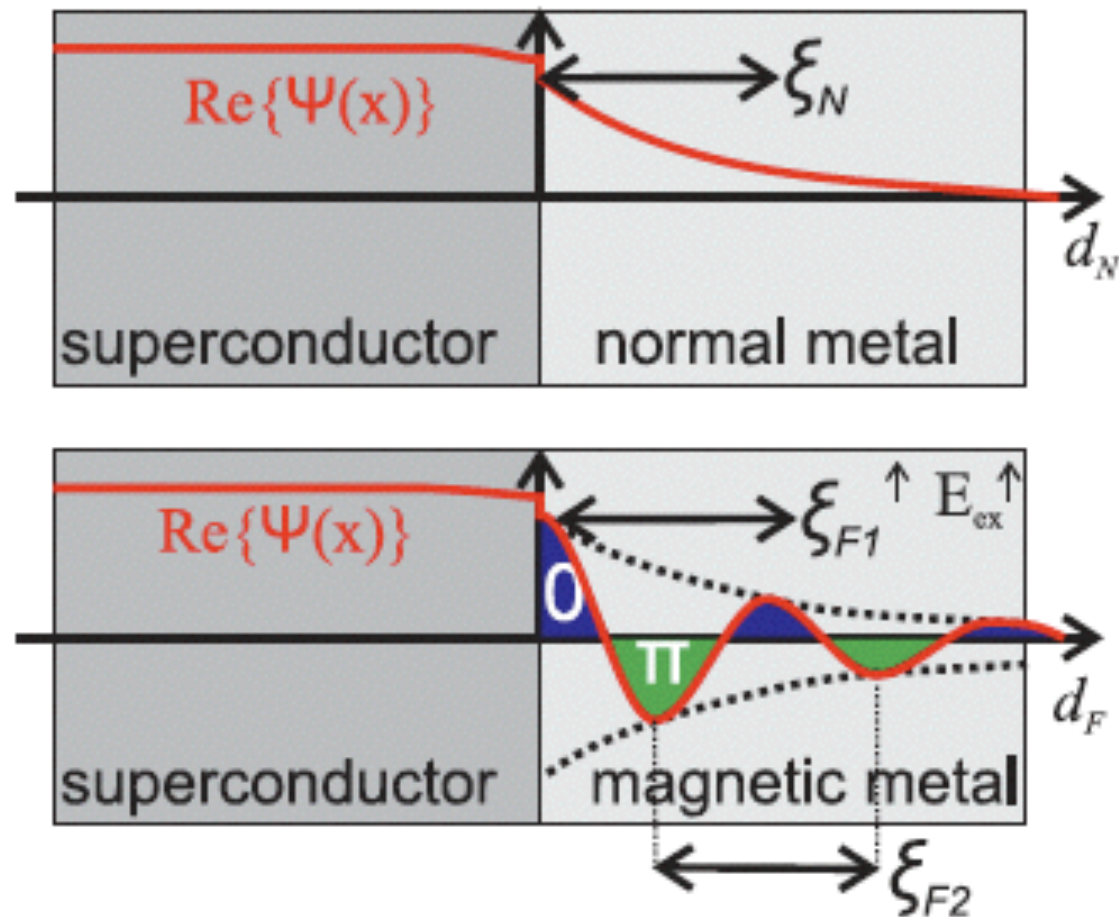
Cooper pair in F $e^{ix\Delta p} |\uparrow\downarrow\rangle - e^{-ix\Delta p} |\downarrow\uparrow\rangle$

$$\text{Re}\Psi = \cos(\Delta p x)$$

Spatial oscillation (FFLO Oscillation)

$$\Delta p = \frac{2E_{\text{ex}}}{\hbar v_F}$$

Proximity effect in S/FM hybrids



SN bilayer

$$\Psi = \Psi_0 \cdot e^{-d_N/\xi_N} \quad \text{Proximity decay}$$

SF bilayer

$$\Psi = \Psi_0 \cdot e^{-d_F/\xi_{F1}} \cos\left(\frac{d_F}{\xi_{F2}}\right)$$

E_{ex} : exchange energy

Proximity decay

Order parameter oscillations

Weides, Martin P. (2006) Josephson tunnel junctions with ferromagnetic interlayer. PhD thesis, Universität zu Köln.

Dirty limit

$$\xi_{F1,2} = \sqrt{\frac{\hbar D}{[E_{\text{ex}}^2 + (\pi k_B T)^2]^{1/2} \pm k_B T}}$$

D: Diffusion constant

E_{ex} : Exchange energy

T: Temperature

Experiments

Ryazanov et al, PRL 86 (2001) 2427

Kontos et al, PRL 89 (2002) 137007

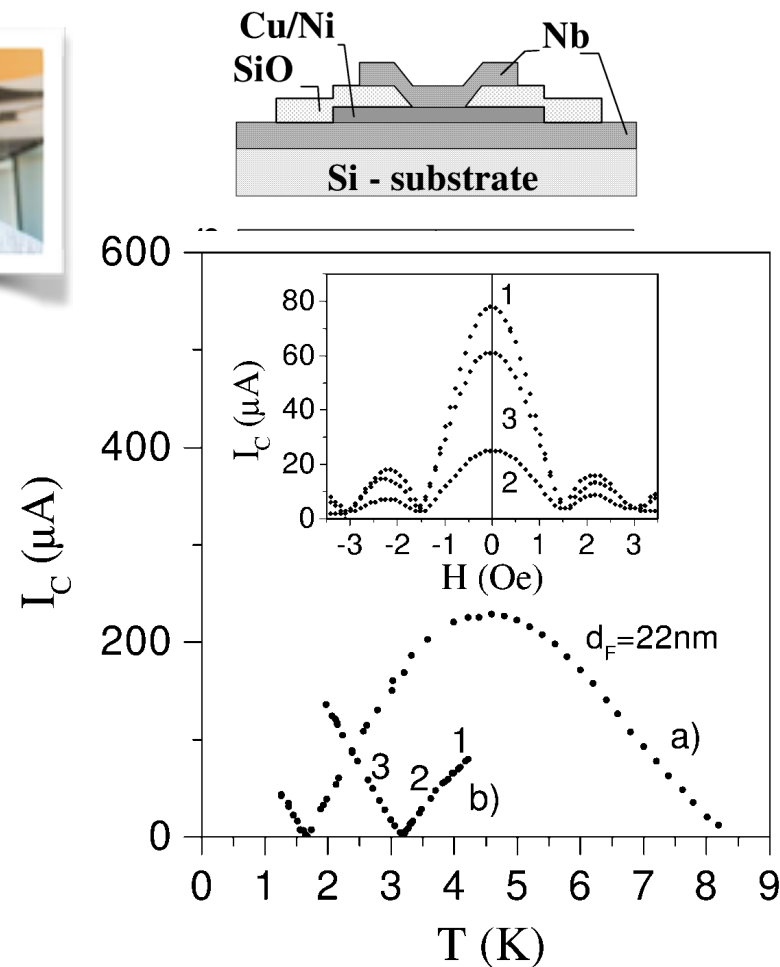
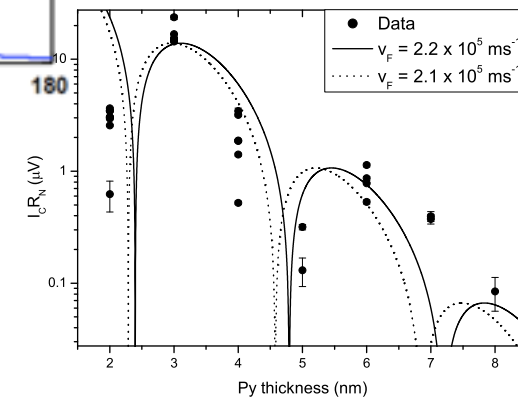
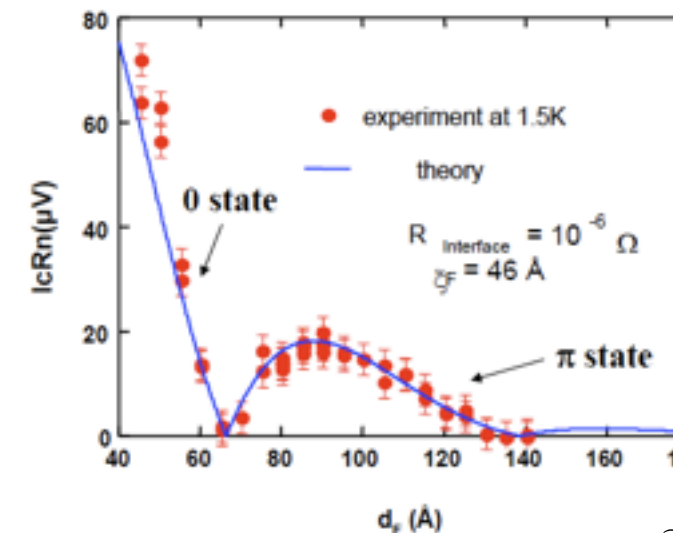
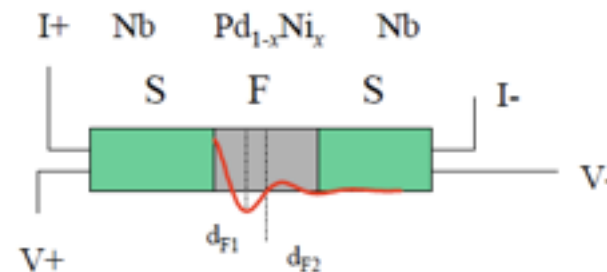


FIG. 3. Critical current I_c as a function of temperature T for two junctions with $\text{Cu}_{0.48}\text{Ni}_{0.52}$ and $d_F = 22$ nm [17]. Inset: I_c versus magnetic field H for the temperatures around the cross-over to the π state as indicated on curve b : (1) $T = 4.19$ K, (2) $T = 3.45$ K, (3) $T = 2.61$ K.



Nb/**CuNi**/Nb
Temperature dependence

Nb/**PdNi**/Nb
FM thickness dependence

Oboznov, Ryazanov, Buzdin (06), Bell, Blamire (06), Weides, Goldobin, Kleiner(06), Birge(09), ...

Applications of π junctions

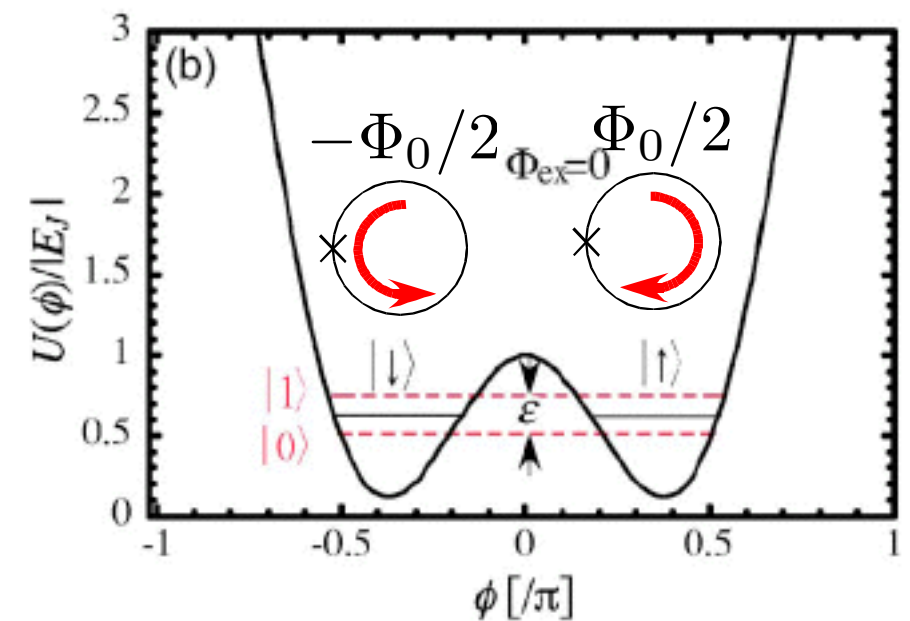
Quiet Qubit

Superconductor ring with single π -junction

Bulaevskii, Kuzii & Sobyannin, JETP Lett. 25 (1977) 291



single-valued nature \rightarrow **Spontaneous circulating current**



Provides natural and precisely-degenerate quantum two-level system
WITHOUT applying external magnetic field

Quiet flux qubit

Ioffe et al, Nature 398 (99) 679

Blatter et al, PRB 63 (01) 174511

Yamashita, Takahashi, Maekawa, PRL 95 (05) 097001

Robust to the fluctuation of external fields

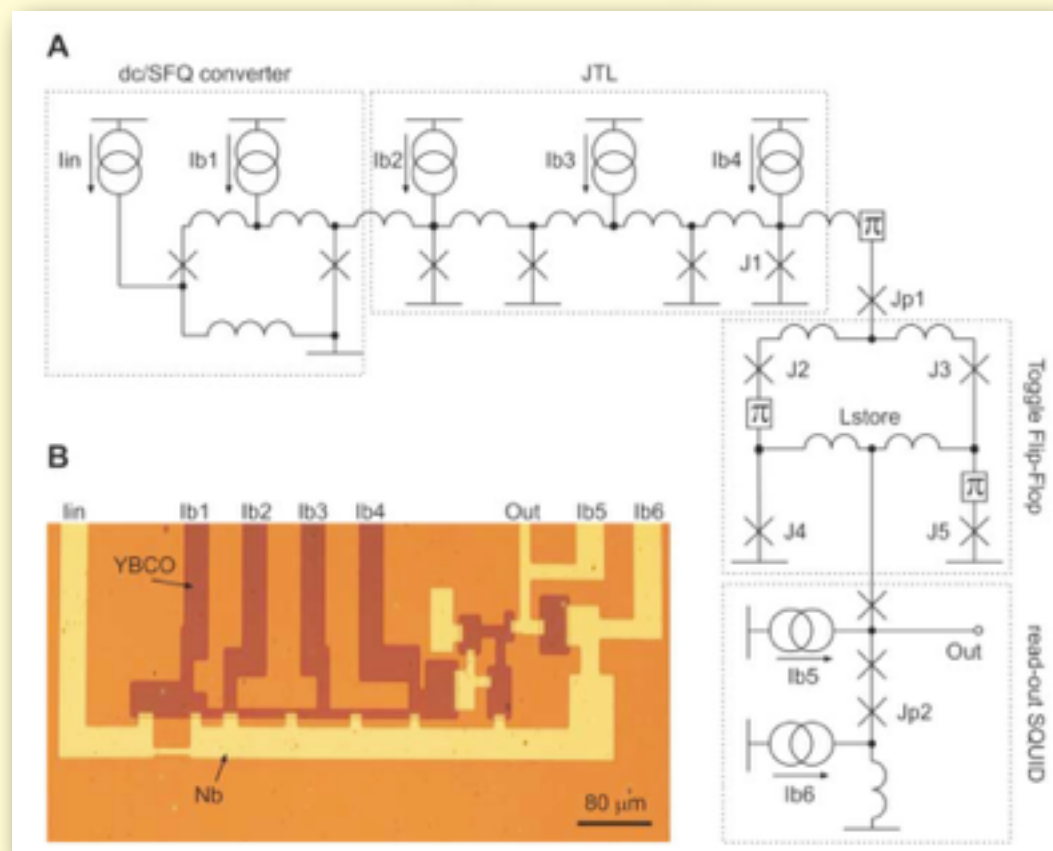
Note: usual flux qubit (0-junction ring): External flux bias is needed

π junction circuits

Classical logic circuit

Ortlepp et al, Science 312 (2006) 1495

Flip flop

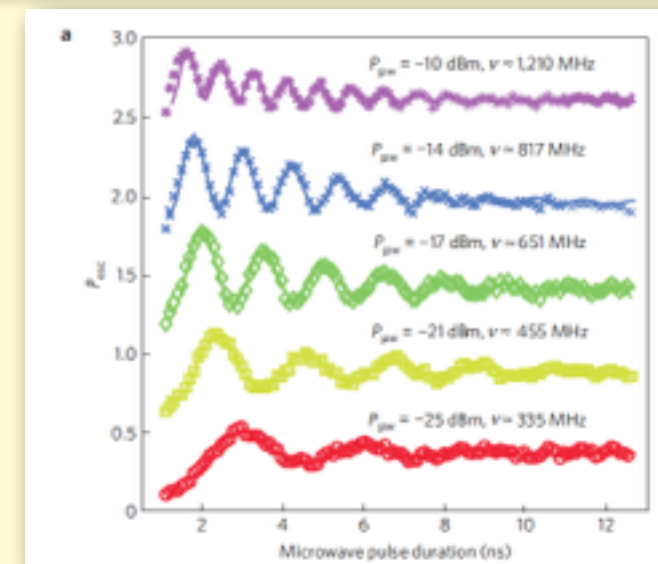
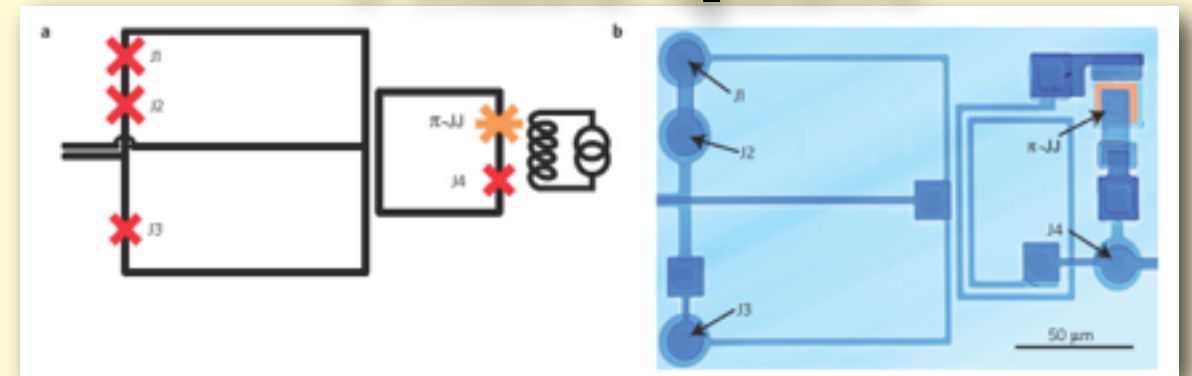


Scalable

Quantum logic circuit

Feofanov Ustinov, et al, Nature Phys. 6 (2010) 593

Phase qubit



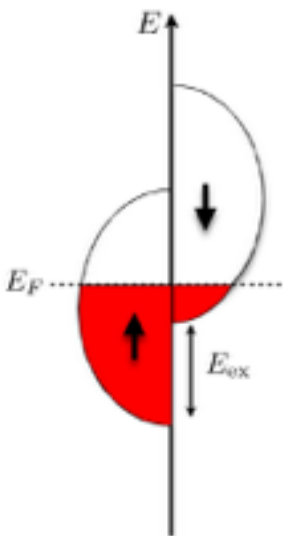
Rabi oscillation

Drawback of FM for quantum applications

FM is a metal → Low energy quasiparticle excitation
→ Strong damping & decoherence

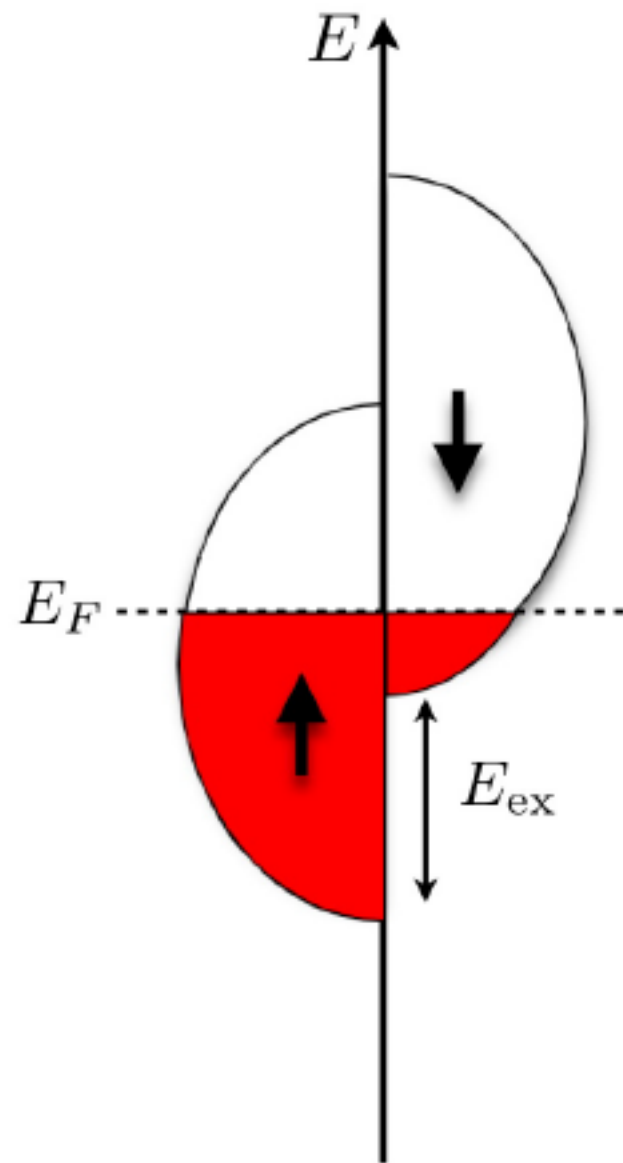


How to avoid? → **Ferromagnetic INSULATORS (FIs)!**

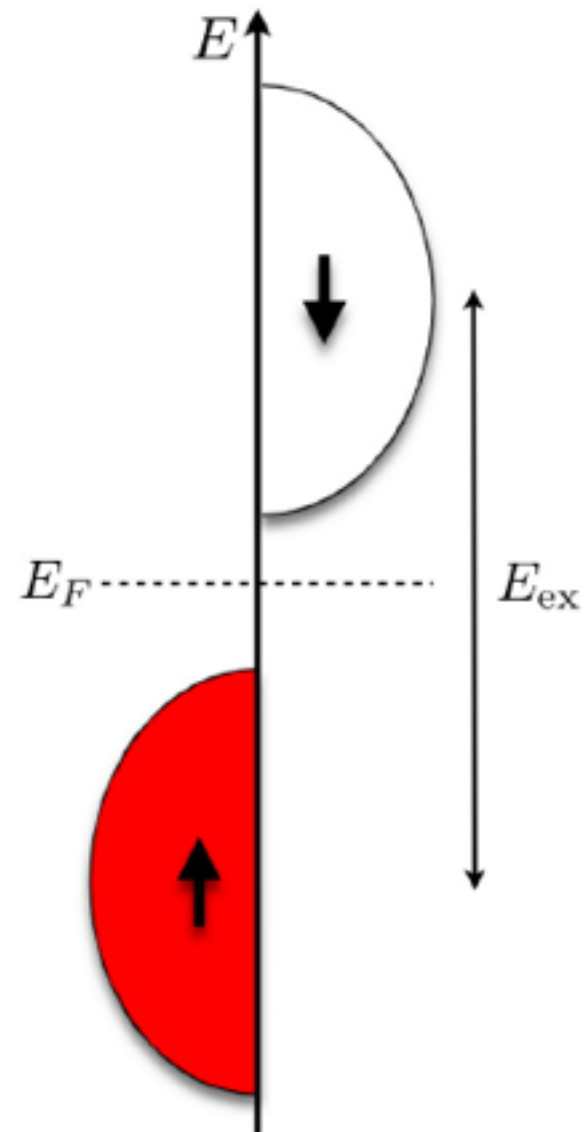


FI based superconducting spintronics for quantum applications

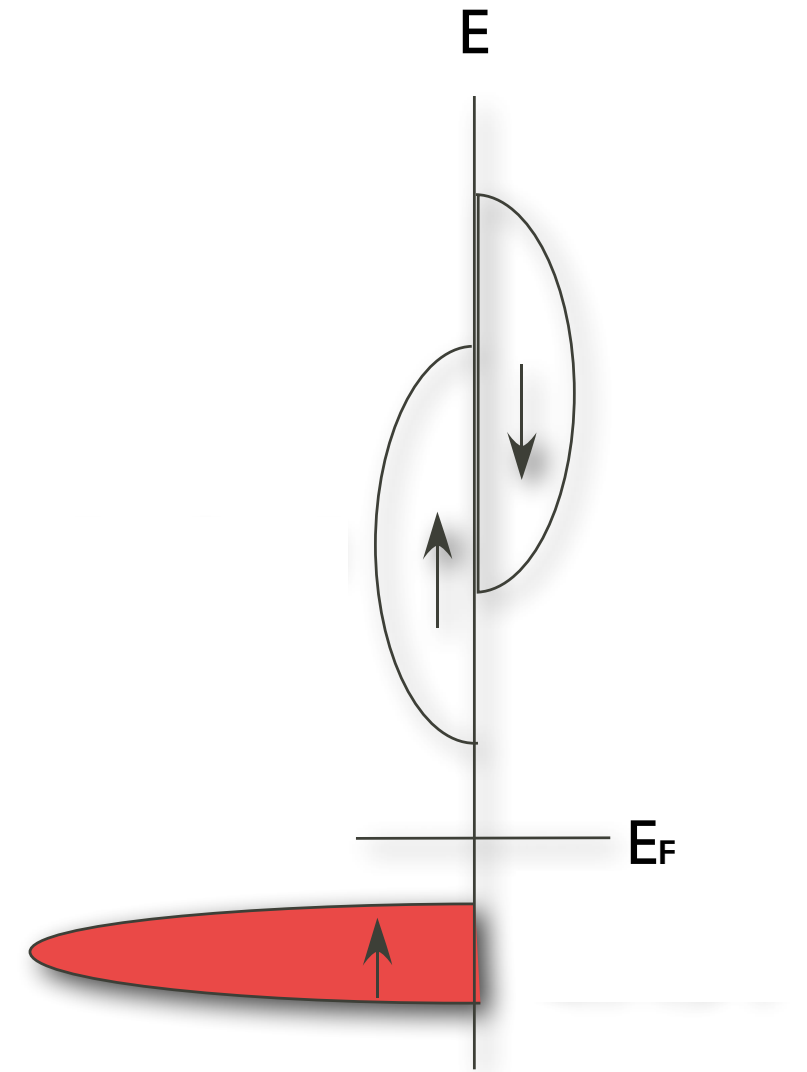
DOS: FM vs FI



FM: Co, Fe, Ni,...



FI: Eu chalcogenides (EuO, EuSe),
Spinel ferrites (NiFe₂O₄),
Oxides (LMO, LBMO, LCMO)...

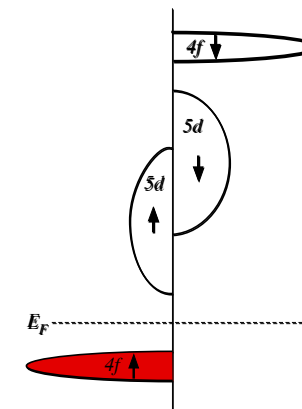
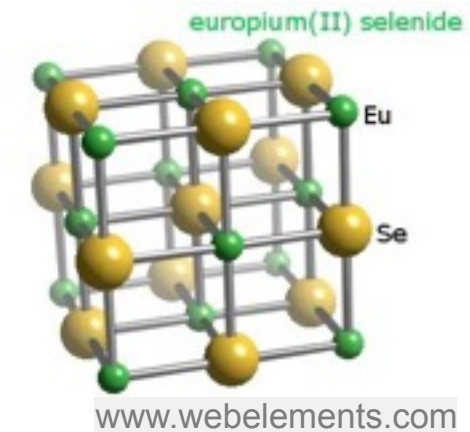


Ferromagnetic insulator

Eu chalcogenides

Table 1. Spin-filter materials.

Material	Magnetic behaviour	T_C (K)	Moment (μ_B)	Structure, a (nm)	E_g (eV)	$2\Delta E_{ex}$ (eV)	P (%)
EuO	FM	69.3	7.9	Fcc, 0.514	1.12	0.54	29
EuS	FM	16.6	7.9	Fcc, 0.596	1.65	0.36	86
EuSe	AFM	4.6	7.9	Fcc, 0.619	1.80		100
BiMnO ₃	FM	105	3.6	Perovskite			22
NiFe ₂ O ₄	Ferri-M	850	2	Spinel	1.2		22
CoFe ₂ O ₄	Ferri-M	796	3	Spinel	0.57		



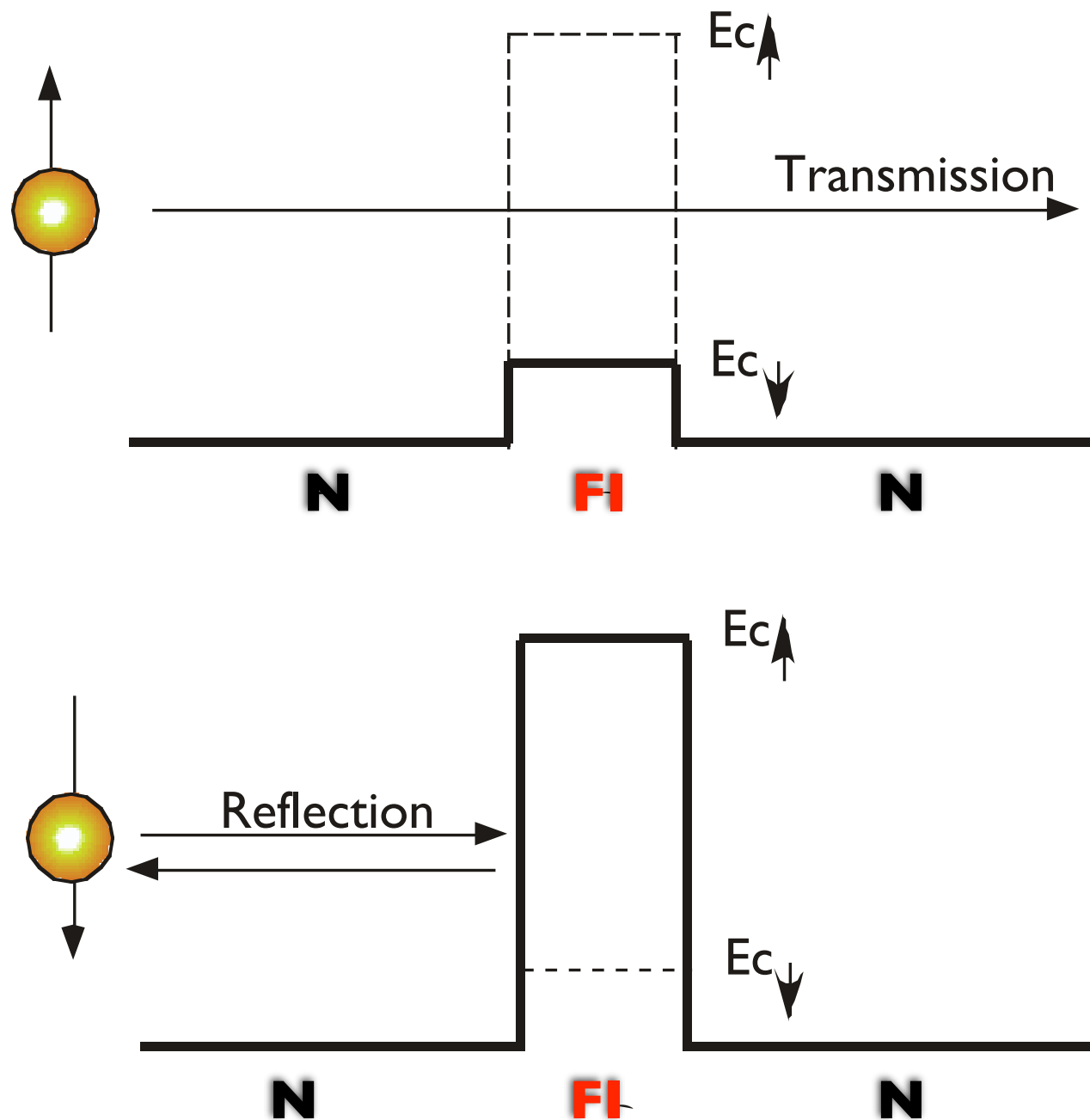
Moodera, Santos & Nagahama J. Phys.: Cond. Mat. 19(2007)165202

→ **Spin filter**

Spin filtering effect

Meservey & Tedrow, Phys. Rep. 238 (1994) 173

G. Prinz, Phys. Today No.4 (1995)58.



Experiments:

Eu chalcogenides (EuO, EuSe),
Spinel ferrites (NiFe_2O_4),
Oxides (LaMnO, LBMO, LCMO)...

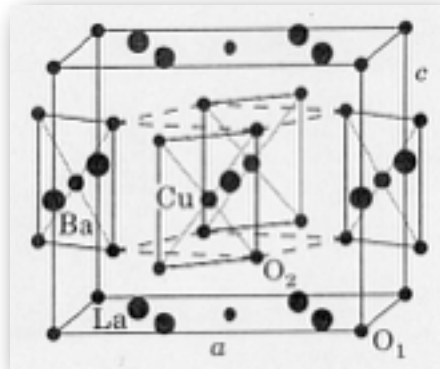
Since the transmission probability depends exponentially on the barrier height, a highly-spin polarized current is generated by the barrier.

$$t_{\uparrow} \gg t_{\downarrow}$$

Spin-selective tunneling = Spin filter

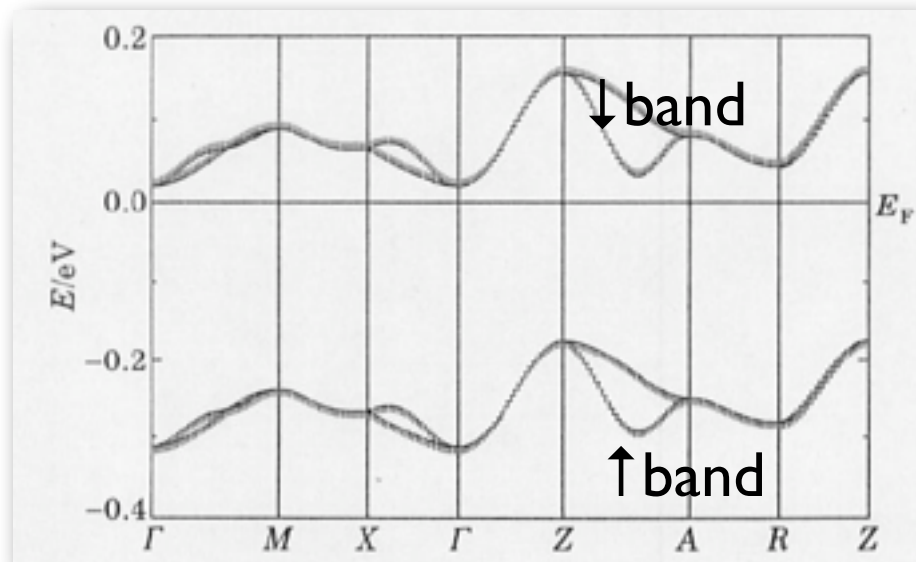
Ferromagnetic Oxide

Oxide ferromagnet



Mizuno et al, Nature 345 (1990) 788

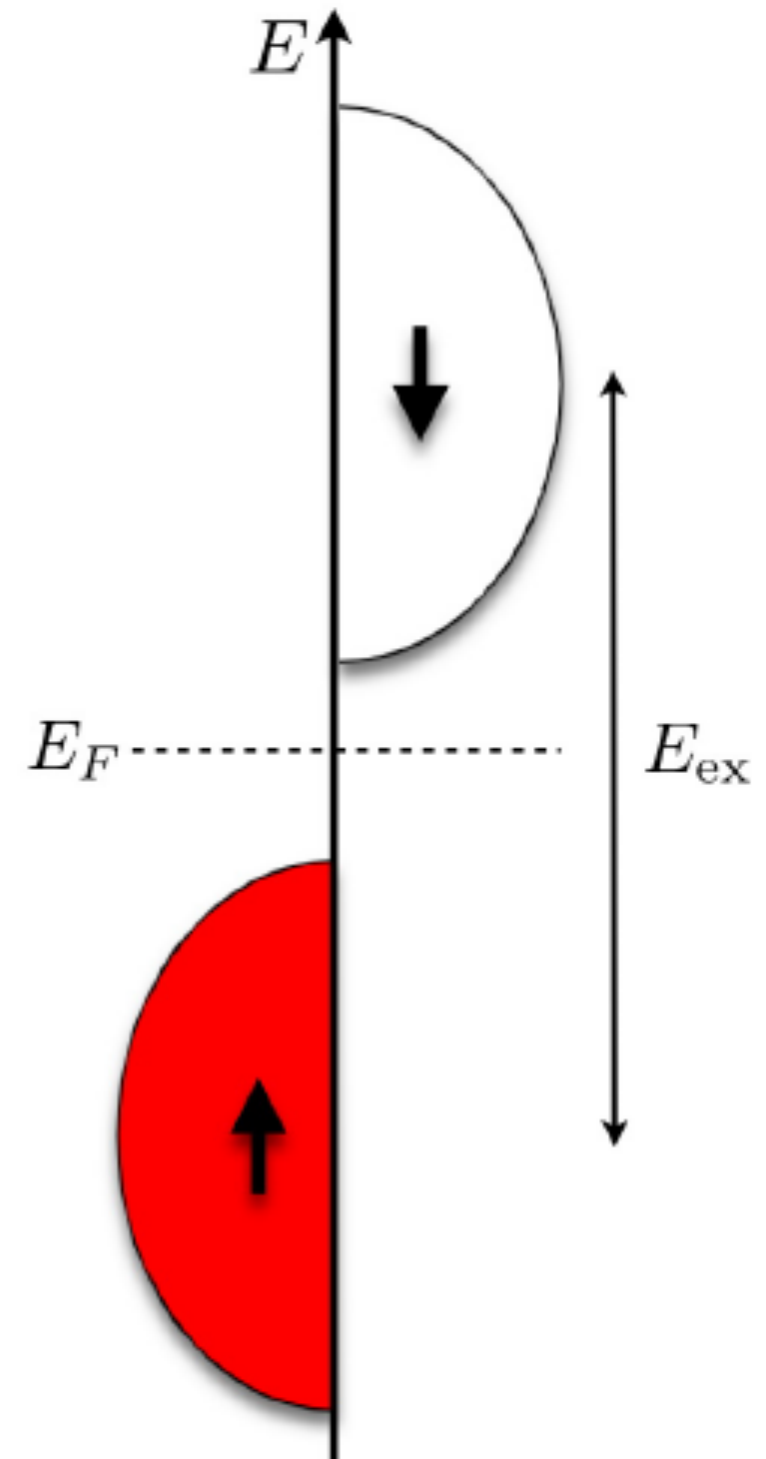
First principle LSDA+U calculation



Both bands (hybridized Cu-d & O-p) are split

$$V_{\text{ex}} \sim 0.34\text{eV}$$

Eyert et al, Europhys. Lett. 31 (1995) 385



FI based superconducting spintronics

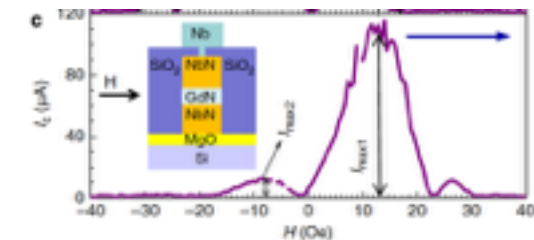
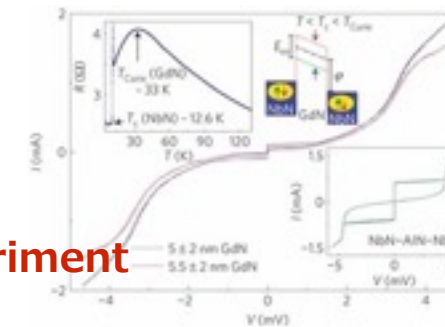
Spin-filter Josephson effect

Kashiwaya & Tanaka Physica 274 (1997) 357

Kawabata & Asano, Int. J. Mod. Phys. **23** (2009) 4320

Senapati, Blamire & Barber, Nature Mat. **10** (2011) 849 **Experiment**

Pal, Barber, Robinson & Blamire, Nature Comm. **5**(2014)3340 **Experiment**



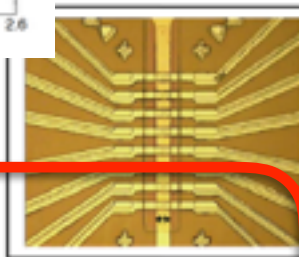
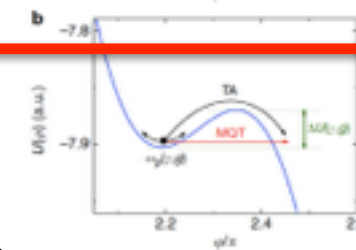
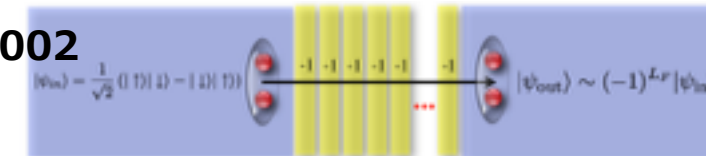
Atomic-scale 0- π transition

Kawabata, Asano, Tanaka, Golubov & Kashiwaya, Phys. Rev. Lett. **104** (2010) 117002

Kawabata, Asano, Low Temp. Phys. **36** (2010) 915 **REVIEW**

Kawabata, Asano, Tanaka & Kashiwaya, Physica E **42** (2010) 1010

Kawabata, Tanaka, Golubov, Vasenko, Kashiwaya & Asano, Physica C **471** (2011) 1199

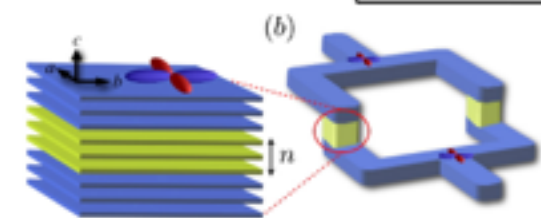


Macroscopic quantum tunneling (MQT)

Kawabata, Kashiwaya, Asano, Tanaka & Golubov, Phys. Rev. B **74** (2006) 180502(R)

Vasenko, Kawabata, Golubov, Kupriyanov, Lacroix, Bergeret & Hekking, Phys. Rev. B **84** (2011) 024524

Massarotti, Pal, Rotoli, Longobardi, Blamire & Tafuri, Nature Comm. **6** (2015) 8376 **Experiment**



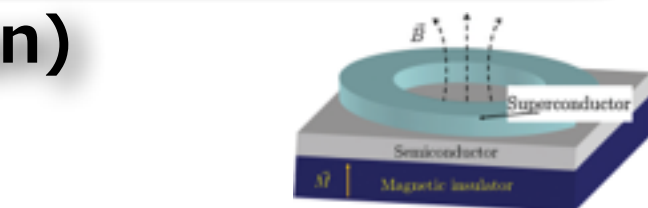
Qubit

Kawabata, Kashiwaya, Asano, Tanaka & Golubov, Phys. Rev. B **74** (2006) 180502(R)

Kawabata, Kashiwaya, Asano & Tanaka, Physica C **427-438** (2006) 136

Kawabata & Golubov, Physica E **40** (2007) 386

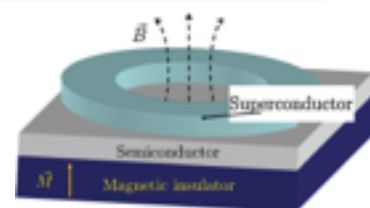
Kawabata, Asano, Tanaka, Kashiwaya & Golubov, Physica C **468** (2008) 701



Majorana fermion & Topological qubit (S/QSHI/FI junction)

Sau, Lutchyn, Tewari & Das Sarma, Phys. Rev. Lett. **104** (2010) 040502

Alicia, Repts. Prog. Phys. **75** (2012) 076501 **REVIEW**



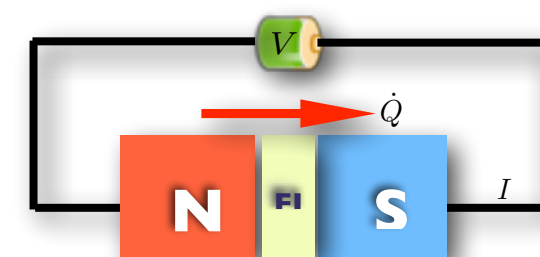
Electron refrigerator & Heat device

Kawabata, Ozaeta, Vasenko, Hekking & Bergeret, Appl. Phys. Lett. **103** (2013) 032602

Kawabata, Vasenko, Ozaeta, Bergeret, & Hekking, JMMM **383** (2015) 157

Linder & Bathen, Phys. Rev. B **93** (2016) 224509

Giazotto et al., Appl. Phys. Lett. **105** (2016) 062602

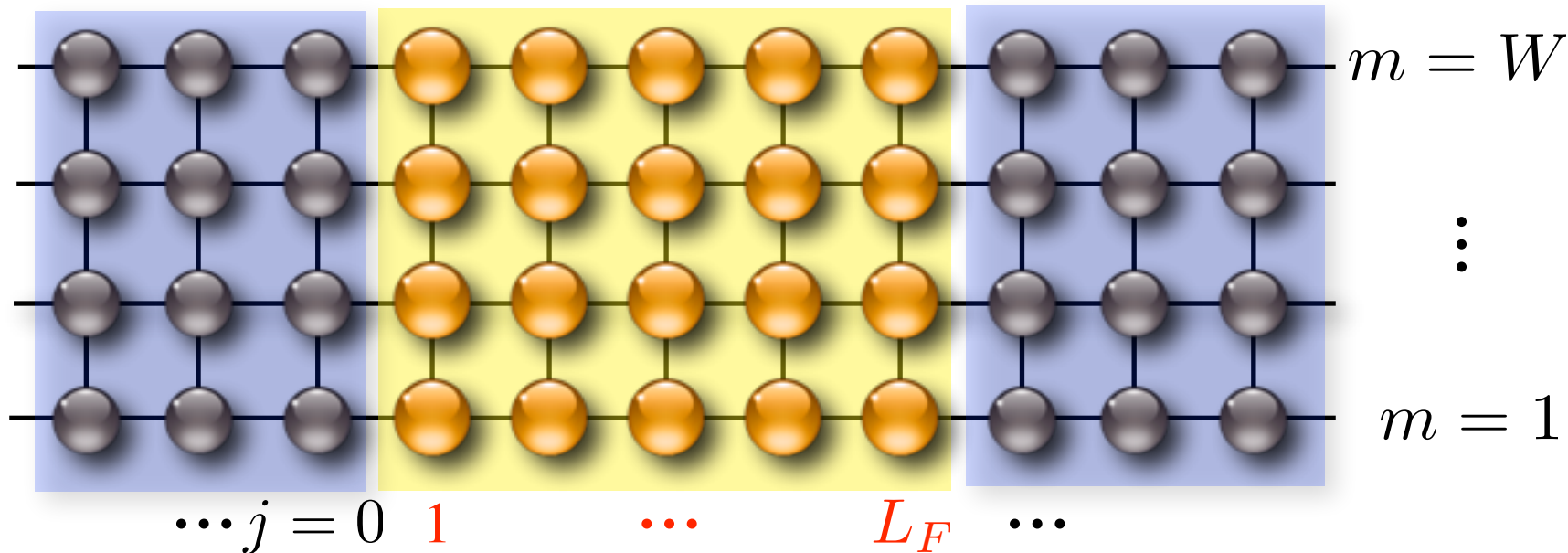


Josephson effect through FIs

Atomic scale 0- π transition

Tight binding BdG calculation

Superconductor **Ferromagnetic insulator** Superconductor (BCS)



$$\mathcal{H}_{\text{BCS}} = \frac{1}{2} \sum_{\mathbf{r}, \mathbf{r}' \in \text{S}} \left[\tilde{c}_{\mathbf{r}}^{\dagger} \hat{h}_{\mathbf{r}, \mathbf{r}'} \tilde{c}_{\mathbf{r}'} - \overline{\tilde{c}_{\mathbf{r}}} \hat{h}_{\mathbf{r}, \mathbf{r}'}^* \overline{\tilde{c}_{\mathbf{r}'}} \right] + \frac{1}{2} \sum_{\mathbf{r} \in \text{S}} \left[\tilde{c}_{\mathbf{r}}^{\dagger} \hat{\Delta} \overline{\tilde{c}_{\mathbf{r}}} - \overline{\tilde{c}_{\mathbf{r}}} \hat{\Delta}^* \tilde{c}_{\mathbf{r}} \right].$$

$$H = -t_n \sum_{\mathbf{r}, \mathbf{r}', \sigma} c_{\mathbf{r}, \sigma}^{\dagger} c_{\mathbf{r}', \sigma} + \sum_{\mathbf{r}} (4t_n - \mu_n) c_{\mathbf{r}, \uparrow}^{\dagger} c_{\mathbf{r}, \uparrow} + \sum_{\mathbf{r}} (4t_n - \mu_n + V_{\text{ex}}) c_{\mathbf{r}, \downarrow}^{\dagger} c_{\mathbf{r}, \downarrow}$$

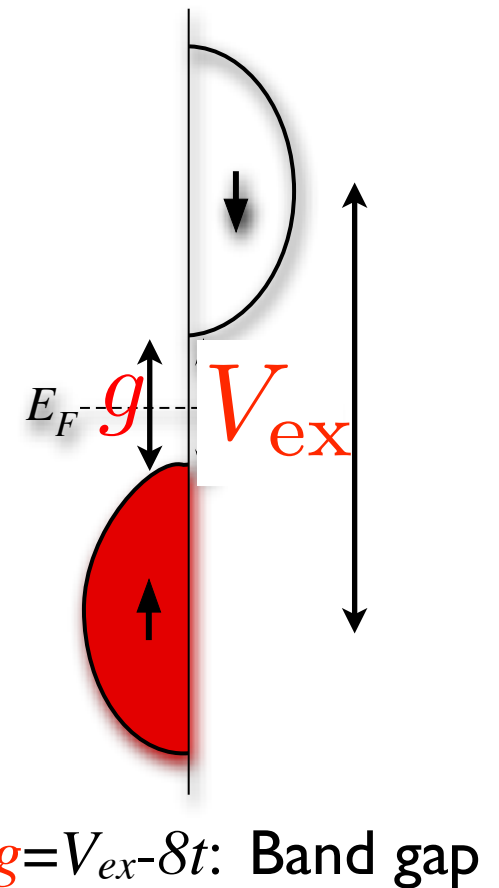
Exchange energy

Bogolibov de-Gennes eq.

Josephson current

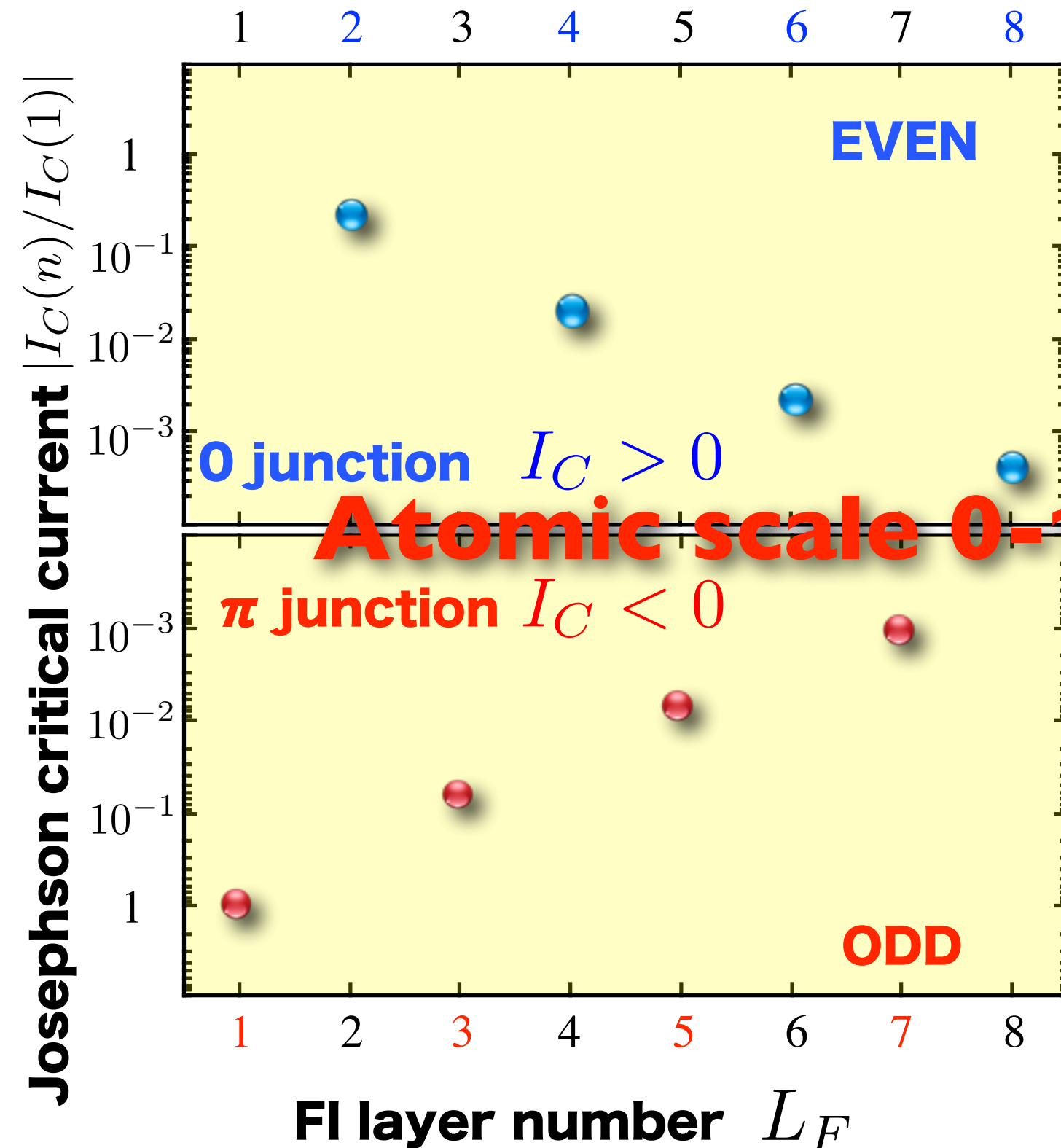
$\varepsilon_n(\phi)$ Andreev levels

$$I_J(\phi) = \frac{2e}{\hbar} \sum_n \frac{\partial \varepsilon_n(\phi)}{\partial \phi} f(\varepsilon_n)$$

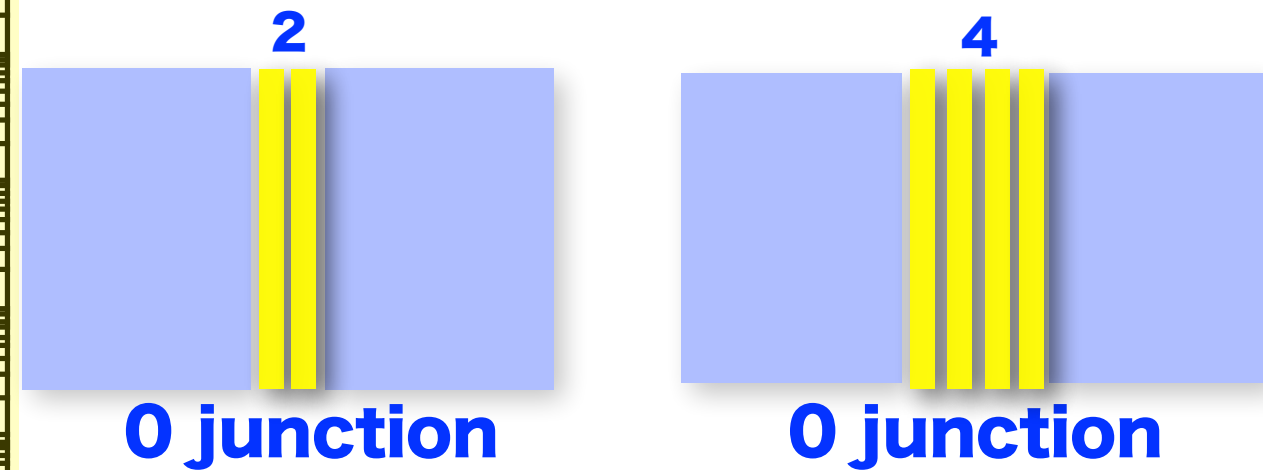


Josephson current

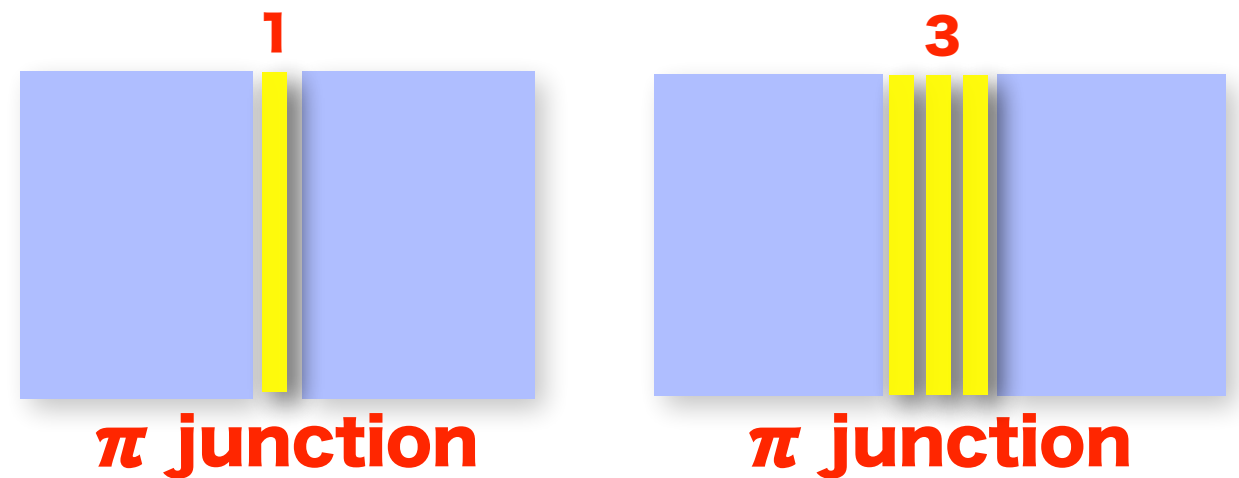
$$I_J = I_C \sin \phi$$



FI layer number = **EVEN**



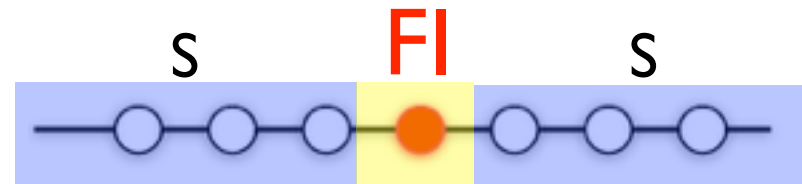
Atomic scale 0- π transition



FI layer number = **ODD**

Origin of π

$$I_C \propto T_{\downarrow}^* T_{\uparrow} \text{ for the tunneling limit } g \gg t$$



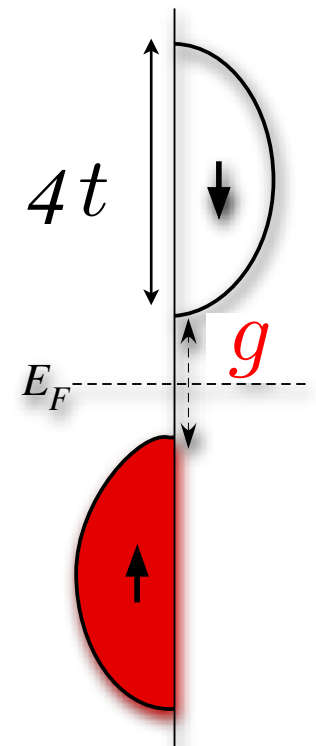
Transmission coefficient of an electron through FI barrier

$$T_{\uparrow} \sim -\frac{t}{g} < 0$$

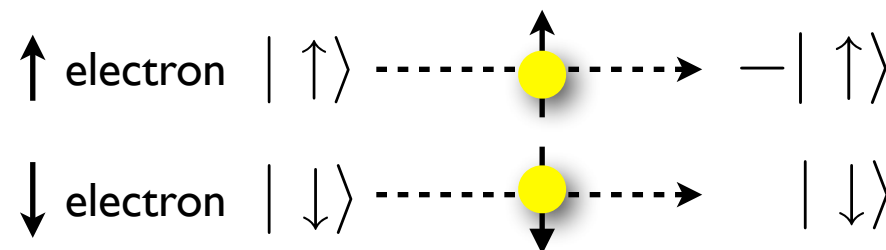
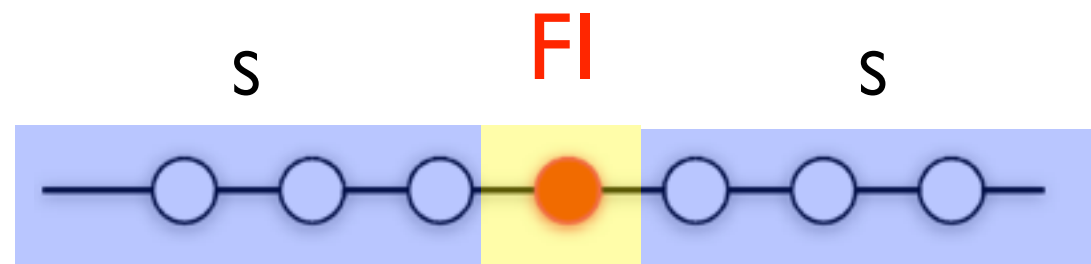
$$T_{\downarrow} \sim +\frac{t}{g} > 0$$

$$\therefore I_C < 0$$

$\therefore \pi$ -junction



Origin of π



Spin-dependent sign change

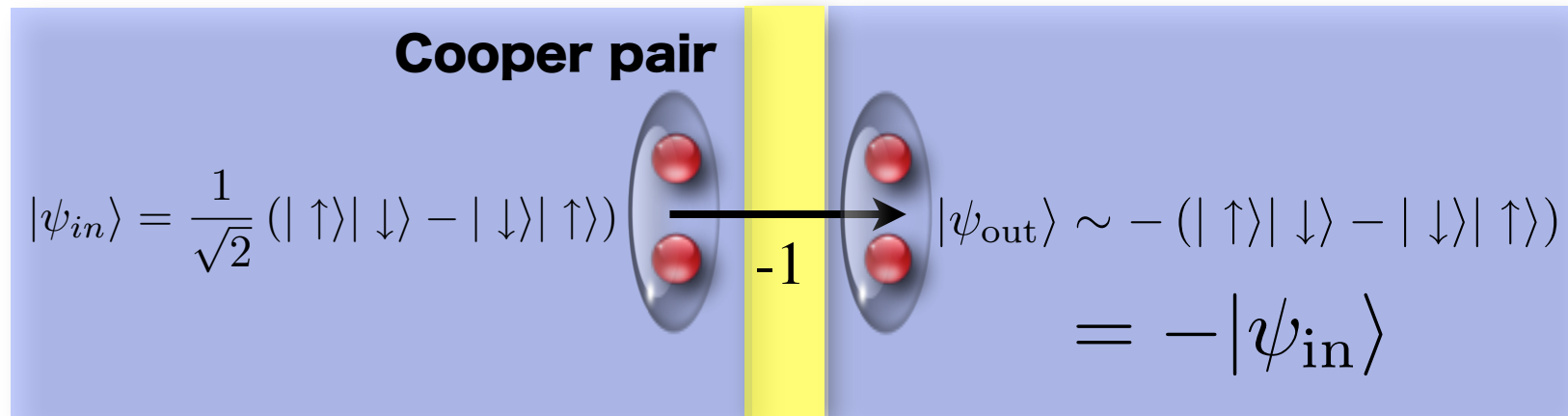
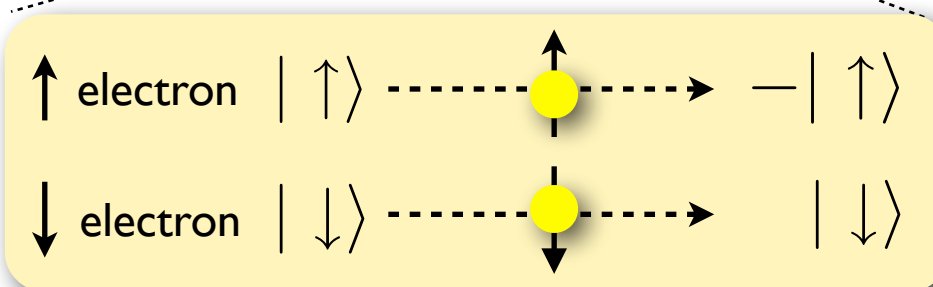
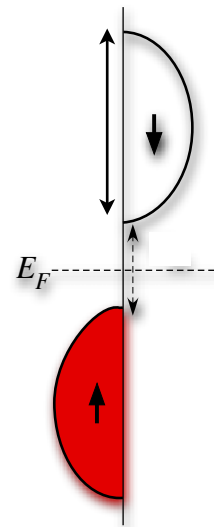
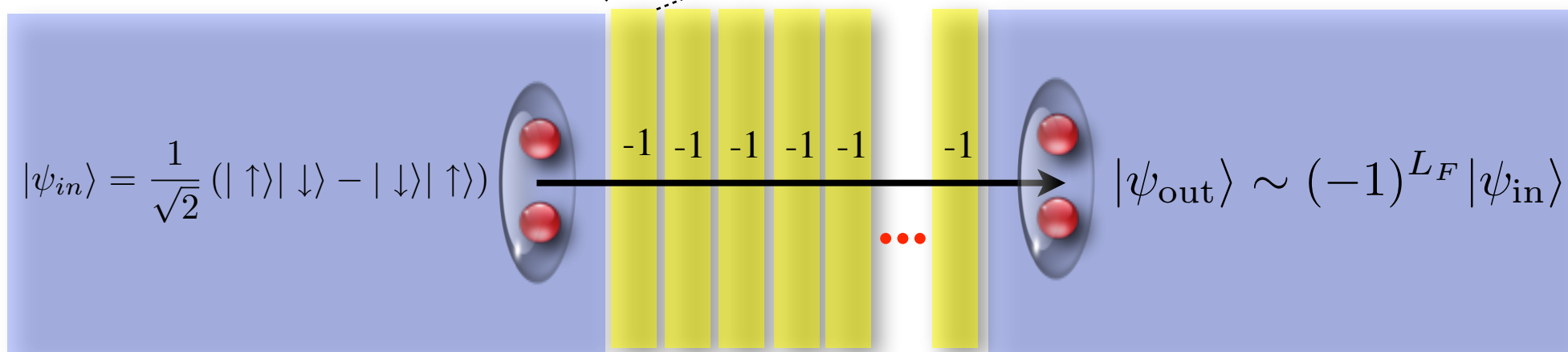
Cuevas & Fogelstrom PRB 64(01)104502

Zhao, et al., PRB 70(04)124510

Kawabata et al., PRL104(10)117002

Cooper pair $|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle \longrightarrow -(|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle)$

π junction

S**FI (single layer)****S** **π -junction****Spin-dependent sign change****FI (L_F layers)****Odd L_F**

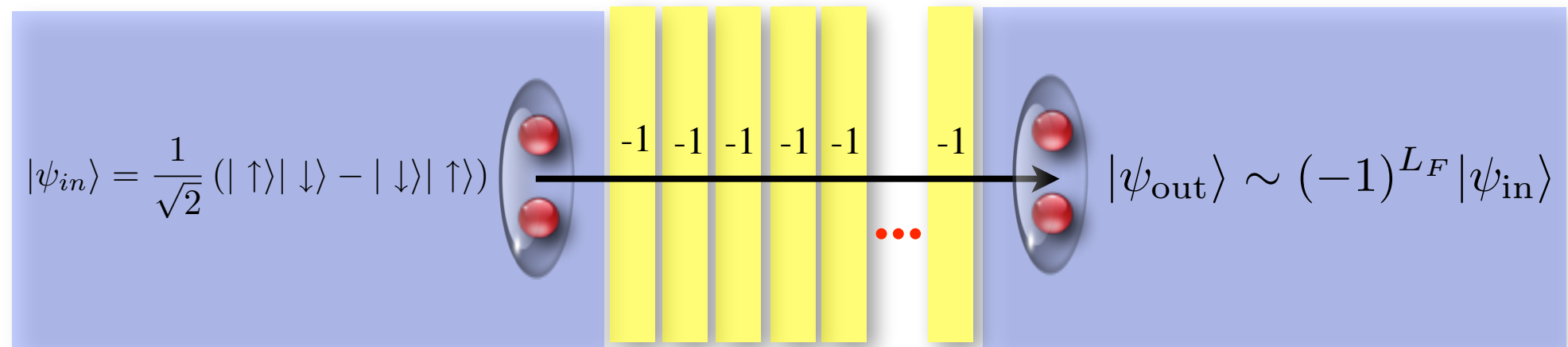
$$I_C < 0$$

 π -junction**Even L_F**

$$I_C > 0$$

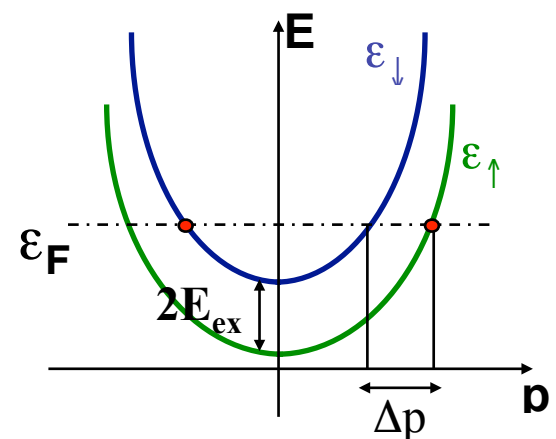
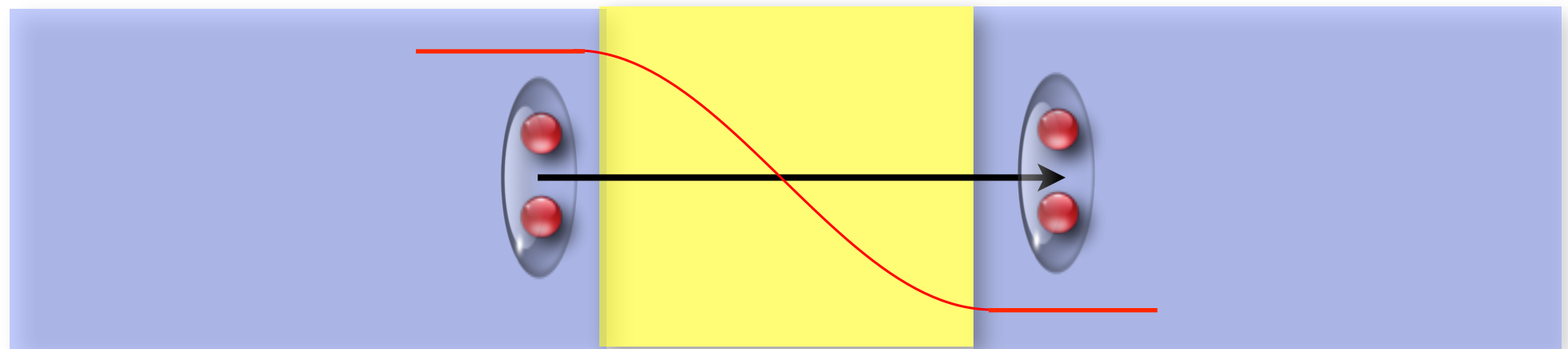
0-junction

FI



Spin-dependent phase shift

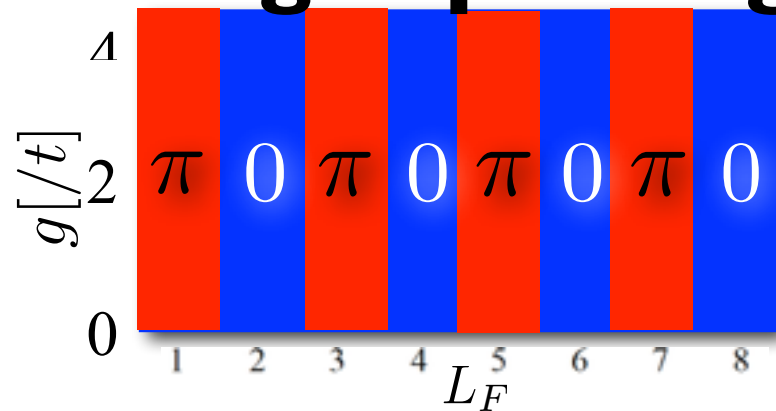
FM



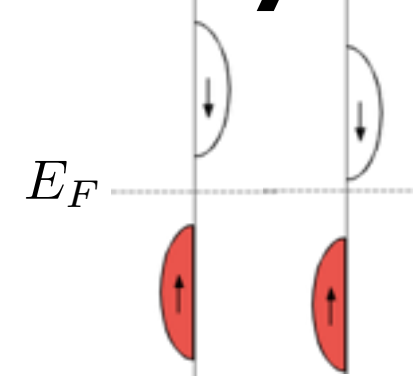
Finite center of mass momentum due to the exchange splitting

Robustness of the atomic scale 0- π transition

Exchange splitting: g

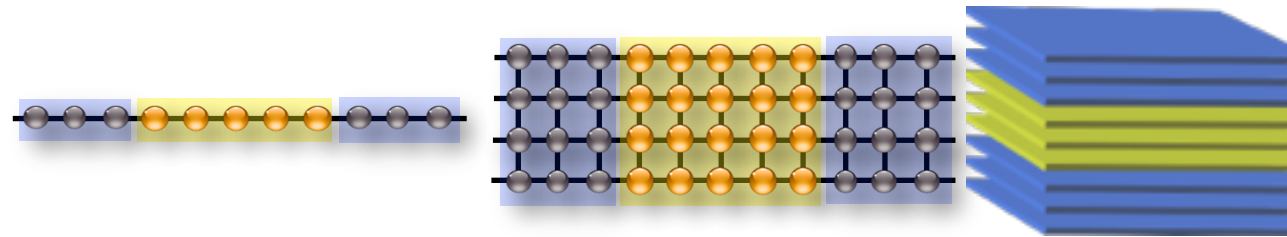


DOS asymmetry



Temperature: T

Dimensionality (1D, 2D, & 3D)



Magnetization configuration (Collinear)



Ferro (uniform)



Anti-ferro

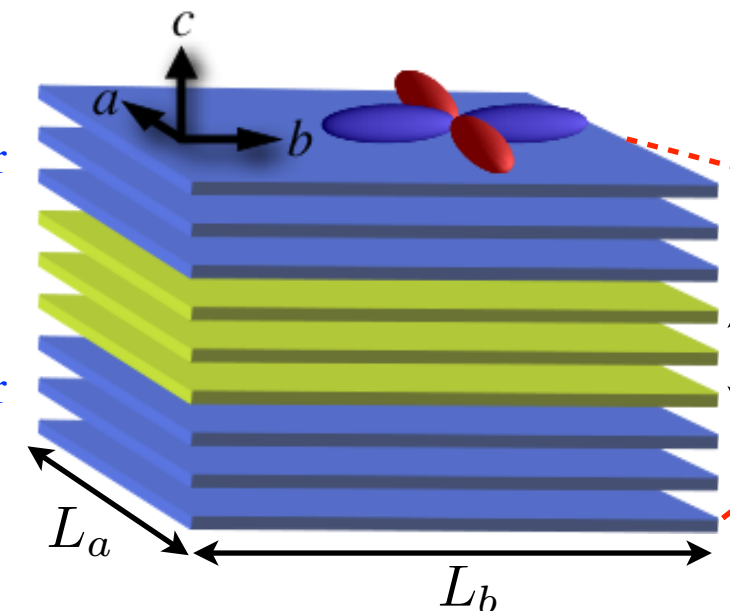
Order parameter symmetry

s-wave JJ & d-wave c-axis JJ

High- T_c layer

FI layer

High- T_c layer



Experiments

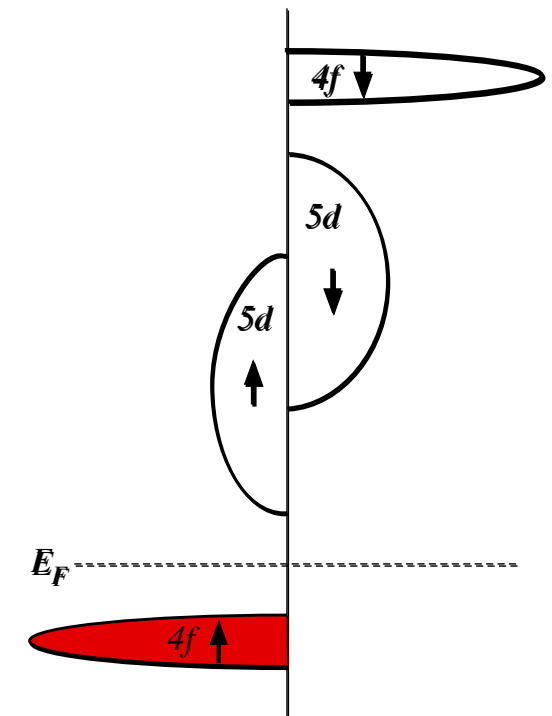
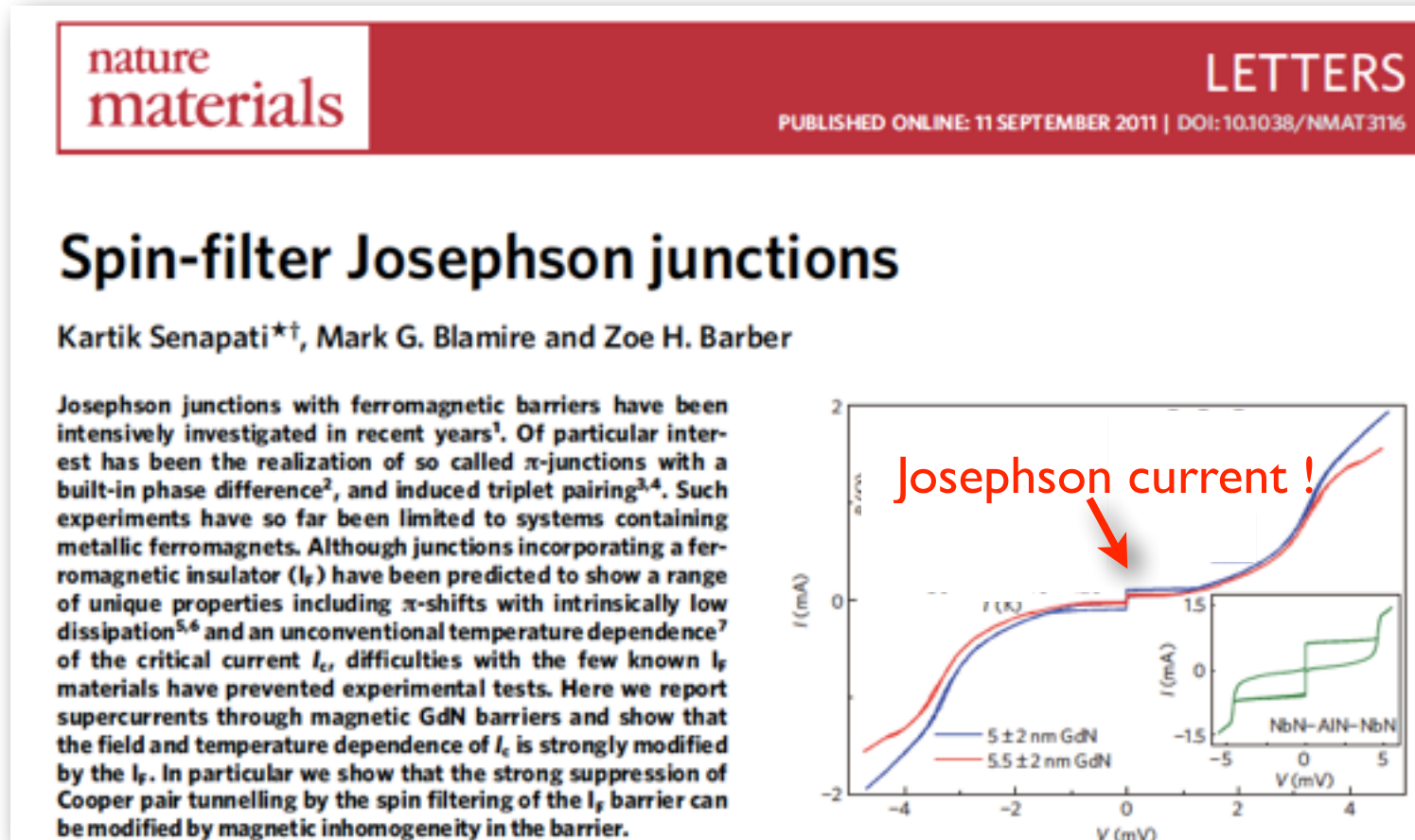


Experiments

NbN/**Spin-filter**(GdN)/NbN

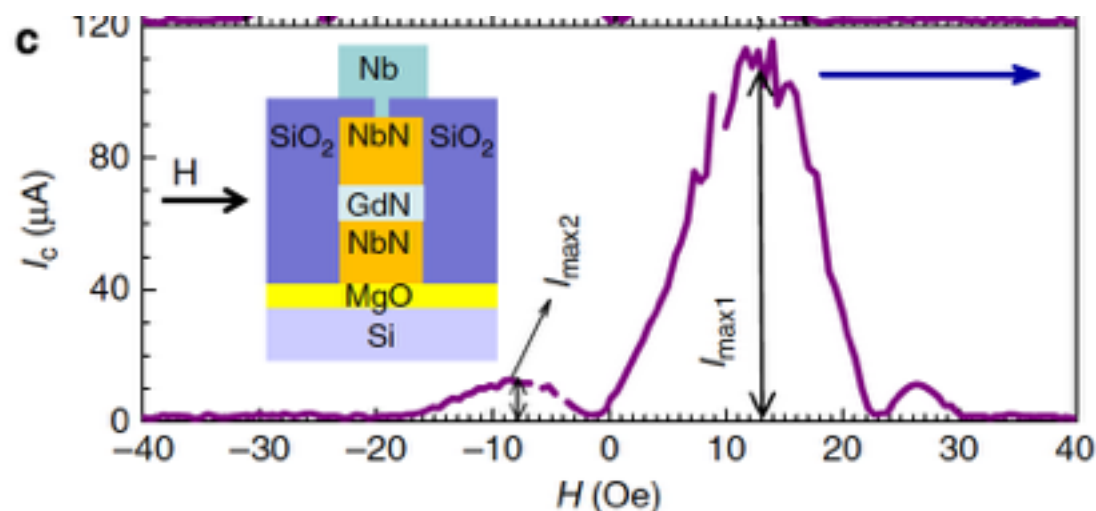
Spin-filter Josephson effect

Senapati, Blamire & Barber, Nature Mat. 10 (2011) 849



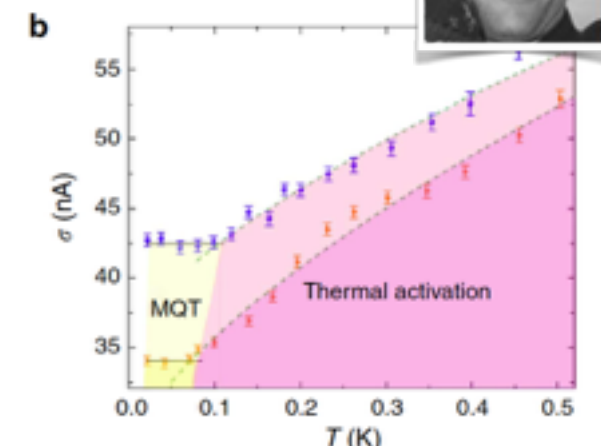
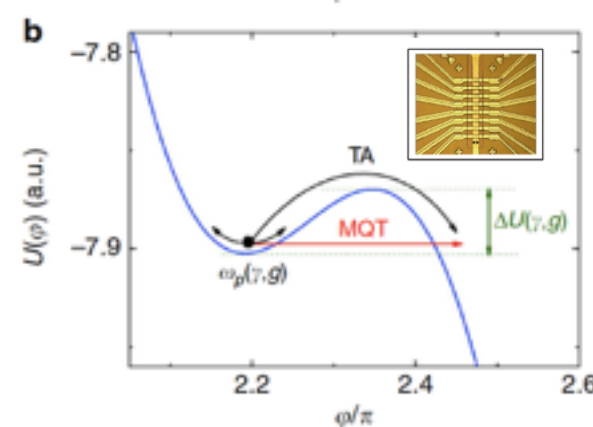
Fraunhofer pattern & Pure 2nd harmonics

Pal, Barber, Robinson & Blamire, Nature Comm. 5(2014)3340



Macroscopic quantum tunneling (MQT)

Massarotti, Pal, Rotoli, Longobardi, Blamire & Tafuri, Nature Comm. 6 (2015) 8376



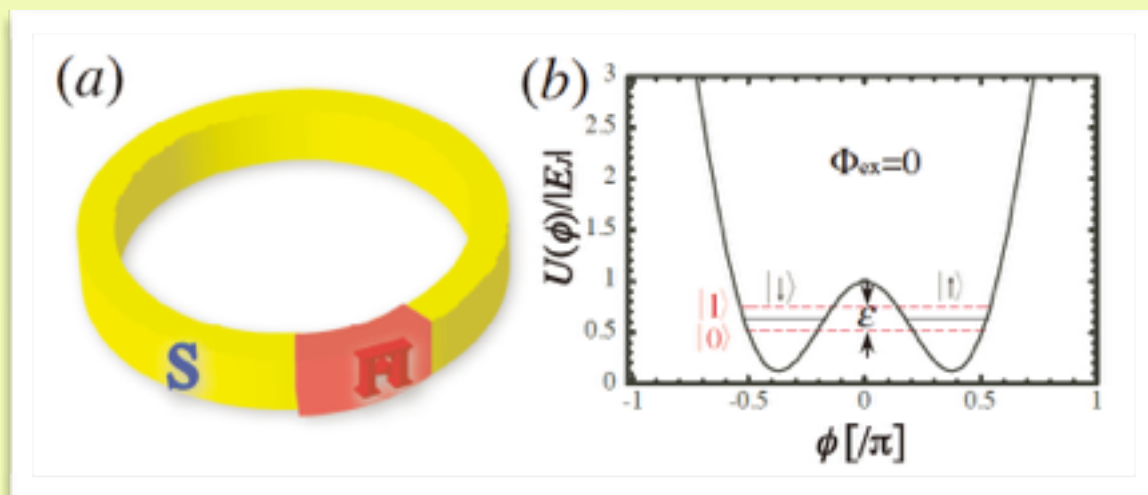
Theory: Kawabata, et al., Phys. Rev. B 74 (2006) 180502(R)

Applications

Quantum application

Coherent π -qubit

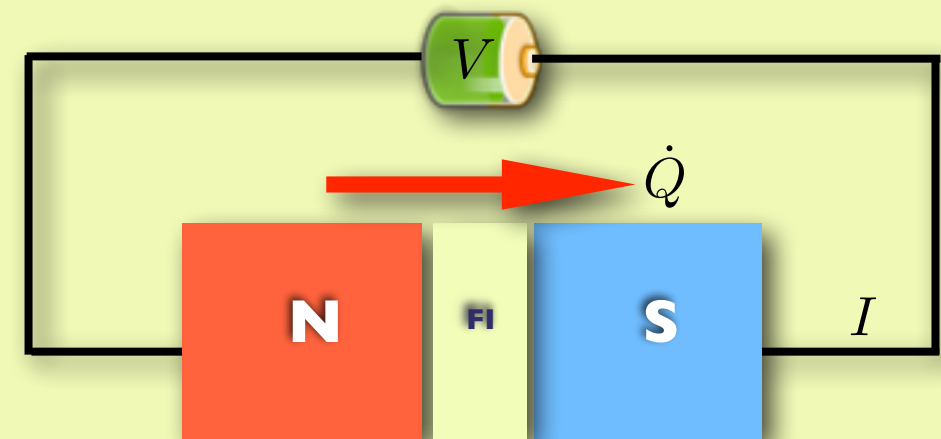
Kawabata, Kashiwaya, Asano, Tanaka & Golubov, Phys. Rev. B 74 (2006) 180502(R)



Highly coherent flux qubit

Electron refrigerator

Kawabata, Ozaeta, Vasenko, Hekking & Bergeret, Appl. Phys. Lett. 103 (2013) 032602



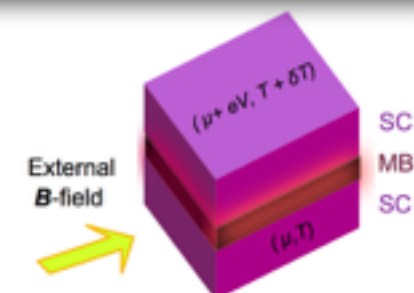
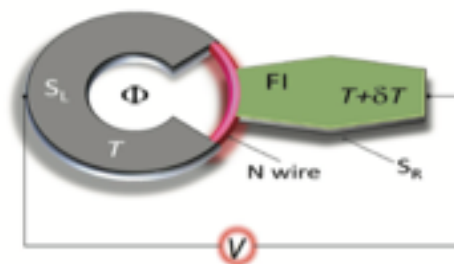
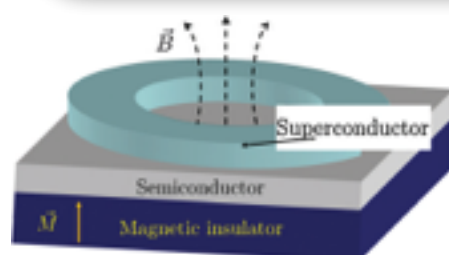
Highly efficient cooler
for quantum devices

Other applications:

Topological qubit: Sau, Lutchyn, Tewari & Das Sarma, Phys. Rev. Lett. 104 (2010) 040502

Heat transistor: Giazotto et al., Appl. Phys. Lett. 105 (2016) 062602

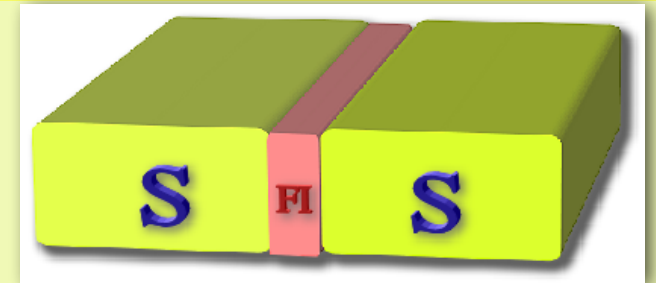
Spin caloritronics: Linder & Bathen, Phys. Rev. B 93 (2016) 224509



Summary

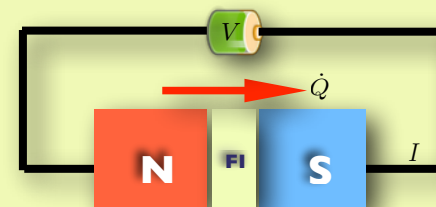
Superconductor spintronics based on ferromagnetic insulators

Josephson effect : Atomic scale $0-\pi$ transition
Macroscopic Quantum Tunneling



Kawabata, Asano, Tanaka, Golubov & Kashiwaya, Phys. Rev. Lett. 104 (2010) 117002
REVIEW: Kawabata & Asano, Low Temp. Phys. 36 (2010) 915

Applications : Coherent qubit & Efficient electron refrigerator



Kawabata, Kashiwaya, Asano, Tanaka & Golubov, Phys. Rev. B 74 (2006) 180502(R)
Kawabata, Ozaeta, Vasenko, Hekking & Bergeret, Appl. Phys. Lett. 103 (2013) 032602
Kawabata, Vasenko, Ozaeta, Bergeret, & Hekking, JMMM 383 (2015) 157

Ferromagnetic-insulator based superconducting-spintronics
would be useful for future QUANTUM & COOLING businesses.